

The financials of renewable power and PPA contracts

Fundamental modelling of power markets

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How can we generate realistic forecasts of future power prices? In the previous article, we have seen that the merit order provides a useful starting point, but lacks sufficient detail for any serious investment analysis or PPA valuation. In this article we explain fundamental power market modelling, which takes us to the required level of detail. It allows us to take into account start costs, energy storage and many more important features of real-life power markets.



Figure 1 shows the main inputs to a fundamental analysis of multiple power markets. Each orange circle or ellipse represents a power market area. The forecast of the power demand, minus the forecast of non-flexible generation from solar, wind and hydro, is the socalled residual load (1). Fuel and CO2 price forward curves (2) and detailed information about power generation assets (3) determine the variable production costs of all flexible generation assets. Note that batteries and other forms of energy

Figure 1: Schematic picture of a fundamental power market model with inputs of three markets. The different elements (1)-(4) are described in the main text. Source: KYOS.

storage should also be included in the power plant list. Finally, interconnection capacities (4) allow power to flow from low-priced areas to high-priced areas until prices are equal in both areas or until the capacity is fully utilized. Of course, there are several more inputs, but these are the main building blocks. In the remainder of this article, we will zoom in on the different elements.





Beyond the merit order

The merit order contains the *variable costs* of the various power generation sources, sorted from low to high. A fuel-fired power plant has different cost components, and it is not straightforward to express the variable costs in a single number. First of all, there are fixed costs, in particular resulting from the original investment (financing costs), but also certain fixed costs to operate the plant and pay the personnel. Fixed costs can be considered 'sunk', meaning that they do not change with the power output.

Secondly, there are variable costs, which move with the power output. The fuel and emission costs are generally the main variable costs, followed by start costs and the variable part of the operations and maintenance costs. Once a power plant has been constructed, only the variable costs determine the optimal dispatch. The optimal dispatch is considerably more complex than the merit order seems to suggest. We take a combined-cycle gas turbine as an example to demonstrate some of the complexity.

Suppose that the higher heating value (HHV) efficiency of the combined-cycle gas turbine (CCGT) is 50%, which means that 2 MWh of natural gas need to be bought in the market for each MWh of power. Natural gas has a carbon (CO₂) content of 0.205 ton per MWh. This means that if the gas price is 15 €/MWh and the carbon emission price 20 €/ton (the cost of emission allowances in the EU ETS), the fuel and emission costs per MWh are:

- Fuel cost = Gas price / Efficiency = 15 / 50%
 = 30 €/MWh
- Carbon cost = Carbon price * Carbon content / Efficiency = 20 * 0.205 / 50% = 8.20 €/MWh

Ignoring any other variable costs, the market price should be at least 38.20 €/MWh for this plant to produce. Or stated differently, if the power price is 45 €/MWh, the gross margin or clean spark spread is 6.80 €/MWh.

Bidding in at variable or marginal costs?

In reality, whether the plant produces, and at what exact output level, depends on more factors than the fuel and emission costs. One element is that the overall efficiency is not constant, but is lower when the plant produces less than its maximum. For example, a gas-fired plant may produce in a range between 180 and 400 MW, with HHV efficiencies rising from 44% to 50%. A higher efficiency results in a lower average cost. Although the average efficiency increases, the marginal efficiency decreases: for each extra MWh of power, progressively more fuel is needed (Figure 2).



Figure 2 Average and marginal costs of production for a gas-fired power plant described in the main text. The green arrow points where the marginal costs of production equal the market power price of 35 €/MWh. It shows that 343 MW is the optimal output level. Source KYOS.

Now suppose the power price is 35 €/MWh, let's consider two possible situations:

- The power plant has no start costs and can turn on or off in each individual hour. This is realistic for a very flexible gas engine. A market price of €35 is not sufficient to recoup the variable costs of 38.20 €/MWh, so the plant will not produce.
- 2. The power plant has to produce in this hour, for example because it cannot turn off for a single hour, or turning off (and later on) is too costly due to start costs.



Now the marginal costs are decisive for the optimal dispatch. When the plant produces 343 MW, its marginal costs are equal to the market price of 35, and hence 343 MW is the optimal dispatch.

Start costs and more

The merit order of a market is a useful albeit simplified picture based on the average variable costs. It can serve as a starting point to assess the potential level of future power prices, but does not reveal everything. Elements that should be considered for fuel-fired plants include:

- The minimum and maximum output levels and efficiencies, as explained in the example
- Start costs, start times and ramp rates
- Minimum on-times and minimum off-times.
- Impact of ambient temperature on efficiencies and output levels.
- Maintenance and unexpected plant trips.
- Must-run obligations, e.g. to generate heat or steam.

The other factors mentioned above are highly dependent on the individual CCGT, but do need to be taken into account in the bidding price. The example shows that it is not easy to derive the prices at which plants bid into the market, even if the market is fully competitive and there is no strategic behavior.

Hydro power and energy storage

The power supply consists of at least three other types of generation: hydro power, energy storage, solar and wind power. Their behavior is very different from fuel-fired generation and is not easily captured in the merit order.

Bidding energy storage into the market is actually quite complex, because it is not the absolute price level that matters, but the relative differences between the hours. With the expansion of renewable (intermittent) power generation, energy storage is becoming increasingly important to balance the system. It is therefore essential to incorporate it in a realistic way in the fundamental model, allowing for a variety of asset parameters, such as:

- Total energy storage capacity (MWh)
- Rate of storage (MWh/h)
- Rate of production (MWh/h)
- Efficiency or energy loss during a full cycle (%)
- Variable costs of operation

Just like the conventional generation assets, the energy storage assets should be optimally dispatched against market prices.

Solar and wind

A fundamental model treats solar and wind power production, together with demand, primarily as non-flexible (intermittent) elements in the power system. They are exogenous inputs to the system optimization. Forecasts of demand and intermittent renewable generation are often derived from economic and policy scenarios, such as published by the IEA, European Commission, EIA, or national governments. Such scenarios generally stipulate future capacities for renewables and a certain percentage change in electricity demand. The challenge is to translate those macro-economic numbers into detailed hourly forecasts.

A common approach is to take a specific historical base year, e.g. 2018, for which the actual hourly demand and renewable production are known. These numbers are then scaled up or down to reflect the forecast growth rates in demand and production. Various refinements are possible, for example to take into account changes in electricity demand profiles or renewable production load factors.





The advantage of taking a specific base year is that it incorporates real-life fluctuations, e.g. due to weather variations. A disadvantage is that the forecast becomes very dependent on what happened in that particular base year. If the base year had a very sunny month of May, then all forecast years will have a very sunny May, with a lot of solar output. To alleviate this problem, it is therefore recommended to run the same analysis with multiple base-years, and average the outcomes across the runs to obtain a single forecast.

Optimization in a fundamental model

Together with the expected future demand and (non-flexible) hydro power production, the expected future solar and wind production are essential ingredients in a power price forecast. Basically, a detailed fundamental model works as follows:

- 1. Forecast residual demand = demand solar/wind/hydro production
- 2. Forecast the fuel and emission prices (via the forward curve or with simulations)
- 3. Find the power price in each hour, such that:
 - a. The output of all flexible generation and storage ≥ residual demand
 - b. All the flexible generation and storage is optimally dispatched against the power prices, taking into account all production costs and (non-)flexibilities; i.e. we find the prices which allow demand to be met in each hour at lowest system cost.

In case of interconnection capacities to other markets, a distinction must be made between the core- and non-core markets. The core-markets are jointly modelled in detail. The use of their interconnection capacities is part of the optimization in step 3. In principle, when the power price in market A is below that in market B, export from A to B must happen until both prices are equal or until the maximum interconnection capacity is utilized. The non-core markets are modelled simpler or not



Figure 3 One iteration in the main part of the optimization algorithm using Dynamic Programming (DP) and Lagrangian multipliers in a fundamental power market model.

at all. In the latter case, in step 1 the forecast net export from core- to non-core markets is added to the demand forecast of the core market.

The optimization in step 3 described above can be fairly complex and time-consuming. Many fundamental models are based on some form of Mixed Integer Linear Programming (MILP). This is a very generic way of formulating the optimization problem, which can then be solved by commercial solvers, such as IBM-CPLEX or Gurobi. A different solution approach is incorporated in the KYOS fundamental model KyPF. It uses dynamic programming and Lagrangian multipliers, following the seminal work by Richard Bellman (1956).

The KyPF model performs different iterations, in which alternately the flexible generation is optimally dispatched (using dynamic programming) and then the hourly power prices (the Lagrangian multipliers) are adjusted depending on the level of imbalance.







Figure 4 The hourly power price forecast of the KyPF model for 14 European countries. The calculation has been performed over an 11-year horizon (2021-2031), but the graph narrowed down to around 2 months. Source: KYOS Analytical Platform.

For example, if the total generation in some hour and iteration is 30,000 MWh, while the residual demand is 32,000 MWh, the price in that hour is lifted with the aim to minimize the imbalance in the next iteration. Adjusting the power prices is simultaneously done for all hours and all markets before a new iteration begins. Typically, around 15 such iterations suffice to reduce imbalances to less than 1% of the residual demand. Over a horizon of around 10 years, and with 14 European 'core' countries with a total of 1,600 flexible power generation assets, the calculation takes around 1.5 hours in the online KYOS Analytical Platform.

These balancing iterations also implicitly capture the costs of balancing the power market in the forecast, which in reality happens on an hour-tohour basis dependent on the supply and demand imbalance. As mentioned in the previous article, the value of renewable PPAs is affected negatively by these balancing costs due to the intermittent nature of power production from solar and wind farms.

Ingredients of a fundamental market model

In a detailed fundamental market model, all elements in a power market are included with sufficient detail and with hourly granularity. Leaving out an essential element, can have a big impact on assumed profitability of a future investment or PPA contract. One such crucial element is the start costs of fuel-fired power plants.

Figure 5 shows the impact of those costs on the German

power prices. The results have been generated with KyPF, the KYOS fundamental power market model. On average, the inclusion of start costs raises the average power prices in 2021 by only 1 €/MWh. Considerably more significant is the impact on the hourly dynamics: with start costs the difference between high- and low price hours becomes larger.



Figure 5 Hourly power prices for the German power market, generated with the KYOS fundamental power market model KyPF. The graph shows the second week of 2021. The inclusion of start costs for fuel-fired plants (blue line) leads to considerably more variation in prices. Source: KYOS Analytical Platform.





A wealth of information

In this article we have explained the principles of fundamental power market modeling. A detailed fundamental model uses relatively detailed inputs of all relevant assets. The non-dispatchable renewable generation (solar, wind, geothermal and part of hydro) enters the model in the form of hourly forecasts over the full evaluation horizon. The fundamental modeler also provides forecasts of fuel and emission prices, forecasts of electricity consumption, and forecasts of interconnection capacities. This requires a lot of data gathering, but is also very rewarding: the end result is not only an hourly power price forecast, but a detailed understanding of how the market could evolve, and plenty of opportunities for sensitivity analysis. In the next article we present a number of practical examples of how this information can be used to assess the financials of renewable power and PPA contracts.

Feedback on our "Financials of renewable Power and PPAs"

We write the articles to share our knowledge and hope it provides a useful source of information for newcomers and experienced professionals alike. Each article will be a mix of qualitative description, some mathematical formulations and numerical examples.

Whether you are buying electricity for your company, developing new projects, working for a utility, providing financing, drafting policies, or just generally interested: we hope you read the articles with interest and share your feedback with us: info@kyos.com.

Renewable production risk management

The PPA module lets the user create and capture any type of renewable PPA. KYOS puts a lot of effort to find the right balance between offering a robust deal capture system and a fully flexible spreadsheet solution. We include standard PPA pricing mechanisms for certain countries and technologies.

Next to that we offer the unique feature that users can add their own pricing structures to the system. For this purpose, we offer an easy-to-use Python programming interface

Advantages KYOS PPA

The KYOS PPA risk management system provides a complete picture of the electricity portfolio with renewable energy PPAs and related hedges. Reporting includes volumetric position, mark-to-market value, value-at-risk and earnings-at-risk.

- All market and forward price curves included
- Flexible deal capturing
- Assess your risk positions and adjust your hedges accordingly
- Extensive capture rate calculator



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